

## Table of Contents

<b>CHAPTER 6: STATISTICS-INVESTIGATE PATTERNS OF ASSOCIATION IN BIVARIATE DATA (2 WEEKS)</b> .....	<b>21</b>
6.0 Anchor Problem: How Much Does Your Brain Weigh? .....	23
SECTION 6.1: CONSTRUCT AND INTERPRET SCATTER PLOTS FOR BIVARIATE DATA.....	25
6.1a Class Activity: Interpret a Scatter Plot.....	26
6.1a Homework: Interpret a Scatter Plot.....	32
6.1b Class Activity: Create and Analyze a Scatter Plot .....	35
6.1b Homework: Create and Analyze a Scatter Plot.....	37
6.1c Classwork: Patterns of Association.....	38
6.1c Homework: Patterns of Association .....	42
6.1d Self-Assessment: Section 6.1.....	45
SECTION 6.2 USE A LINEAR MODEL TO SOLVE PROBLEMS .....	46
6.2a Class Activity: Fit a Linear Model to Bivariate Data .....	47
6.2a Homework: Fit a Linear Model to Bivariate Data.....	53
6.2b Class Activity: Tongue Twister.....	60
6.2b Homework: Tongue Twisters Equations.....	62
6.2c Self-Assessment: Section 6.2.....	63
SECTION 6.3 CONSTRUCT AND INTERPRET TWO-WAY FREQUENCY TABLES TO ANALYZE CATEGORICAL DATA .....	64
6.3a Class Activity: Construct Two-Way Frequency Tables using Categorical Data .....	65
6.3a Homework: Construct a Two-Way Frequency Table.....	70
6.3b Class Activity: Interpret Two-Way Frequency Tables .....	73
6.3b Homework: Interpret Two-Way Frequency Tables.....	76
6.3c Class Activity: Conduct a Survey.....	80
6.3d Self-Assessment: Section 6.3.....	82

# Chapter 6: Statistics-Investigate Patterns of Association in Bivariate Data (2 weeks)

## Utah Core Standard(s):

- Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. (8.SP.1)
- Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line. (8.SP.2)
- Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. *For example, in a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height.* (8.SP.3)
- Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. *For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?* (8.SP.4)

**Academic Vocabulary:** Experiment, outcomes, sample space, random variables, realizations, quantitative (numerical) variables, categorical variables, univariate data, bivariate data, scatter plot, association, positive association, negative association, no (zero) association, perfect association, linear association, non-linear association, cluster, outlier, line of best fit, linear model, two-way frequency table, marginal frequencies, relative frequencies.

## Chapter Overview:





Up to this point, students have been studying data that falls on a straight line. Most of the time data given in the real world is not perfect; however, often the data is associated with patterns that can be described mathematically. In this chapter, students will investigate patterns of association in quantitative bivariate data by constructing and interpreting scatter plots, fitting a linear function to scatter plots that suggest a linear association, and using the function to solve problems and make predictions. In addition they explore categorical bivariate data by constructing and interpreting two-way frequency tables.

## Connections to Content:

**Prior Knowledge:** In 6<sup>th</sup> and 7<sup>th</sup> grade students analyzed and interpreted data that was univariate, in 8<sup>th</sup> grade their analysis continues in the interpretation of bivariate data. As they view a scatter plot they use the tools and skills of graphing and writing linear equations to create an equation for the linear model exhibited by their lines of best fit. Also they use their linear model to make predictions about the data.

**Future Knowledge:** The study of bivariate data collection and analysis is further explored in Secondary Math I. Students will more formally fit a line to bivariate data by not only finding the regression equation but also calculating correlation coefficients and making residual plots to formally assess the fit of the model. They also will do this for nonlinear models. Also the study of two-way frequency tables is expanded to looking at marginal and joint frequencies more formally.

## MATHEMATICAL PRACTICE STANDARDS (emphasized):

	<p><b>Make sense of problems and persevere in solving them.</b></p>	<p>1. Emina loves to eat tomatoes from her garden in Salt Lake City. She asked her friend Renzo, “Don’t you just love tomatoes?” Renzo crinkled his nose and replied, “Ew, tomatoes gross me out! When I see them in the grocery store, I just keep on walking.” Renzo’s response prompted Emina to think, “I don’t buy tomatoes at the grocery store either, because I grow them in my garden. The tomatoes from my garden are delicious, whereas grocery store tomatoes look less appealing to me. I wonder if there is an association between enjoying tomatoes and having a garden at home?”</p> <p><i>In the problem above the student must help Emina determine if there is an association between liking tomatoes and having a garden at home. They organize collected data into a two-way frequency table and then analyze it. Students must problem solve as they decide how to organize their data and as they determine what the data is telling them.</i></p>
	<p><b>Model with mathematics.</b></p>	<p>Students will say a selected tongue twister one at a time. In the first trial, only the first student will say the tongue twister; in the second trial, only the first and second students will say the tongue twister, etc. In each trial, one person will be added to the chain of tongue twisters and the total elapsed time will be recorded.</p> <p>Tongue twisters:</p> <ul style="list-style-type: none"> <li>A. Work will win when wishy-washy wishing won’t.</li> <li>B. Three witches wished three wishes, but which witch wished which wish.</li> <li>C. Peter Piper picked a peck of pickled peppers.</li> <li>D. Picky people pick Peter Pan peanut butter it is the only peanut butter picky people pick.</li> </ul> <p><i>Throughout the chapter students will fit a linear model to several real-life situations. In the task above students create a linear model through a scatter plot and line of best fit of the time it takes to say a tongue twister. In addition, they create an equation for the linear model to make predictions about the data.</i></p>
	<p><b>Construct viable arguments and critique the reasoning of others.</b></p>	<p><i>Throughout the chapter, students are asked to create a scatter plot and analyze the scatter plot to determine if there is an association between two variables. They look for trends and patterns, including clusters and outliers. They provide explanations related to the context for the associations, trends, and patterns. field goals attempted and field goals made. Students are making <b>arguments</b> about the data and are asked to <b>support</b> their arguments with data and critical thinking about the context and limitations of the data.</i></p>
	<p><b>Use appropriate Tools Strategically</b></p>	<p><i>An important component to creating and analyzing a linear model is through graphing software. An online graphing software or graphing calculator can be used to create a line of best fit and a regression equation. In the problem above students test their ability to make a line of best fit for a scatter plot by comparing it to the computer’s line. They also use the software to make predictions about the data.</i></p>

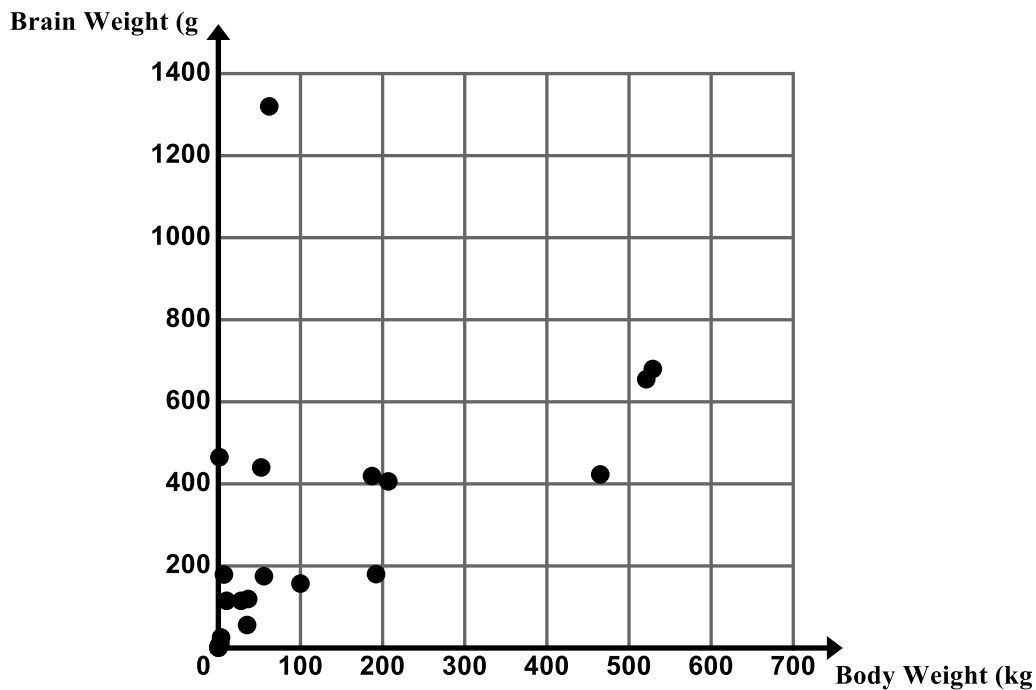
## 6.0 Anchor Problem: How Much Does Your Brain Weigh?



The following table shows the Animal Weight versus Animal Brain Weight for several animals.

Body and brain weight by animal. Source: <a href="http://mste.illinois.edu/malcz/DATA/BIOLOGY/Animals.html">http://mste.illinois.edu/malcz/DATA/BIOLOGY/Animals.html</a>		
Animal	Body Weight (kg)	Brain Weight (g)
Mountain beaver	1.35	465
Cow	465	423
Grey wolf	36.33	119.5
Goat	27.66	115
Guinea pig	1.04	5.5
Donkey	187.1	419
Horse	521	655
Potar monkey	10	115
Cat	3.3	25.6
Giraffe	529	680
Gorilla	207	406
Human	62	1320
Rhesus monkey	6.8	179
Kangaroo	35	56
Golden hamster	0.12	1
Mouse	0.023	0.4
Rabbit	2.5	12.1
Sheep	55.5	175
Jaguar	100	157
Chimpanzee	52.16	440
Mole	0.122	3
Pig	192	180

The following is a scatter plot of the data.



- a. Is there an association between an animal's body weight and its brain weight? Describe any trends or patterns you observe in the data including clusters and outliers.
- b. Draw a line of best fit for the data and write an equation for your line of best fit.
- c. Explain the meaning of the slope and y-intercept in the context.
- d. Use your prediction equation to predict the brain weight of an African Elephant. The average African Elephant weighs 6,654 pounds.
- e. The actual average brain weight of an African Elephant is 5,712 grams. How does your prediction compare to the actual average weight of an African Elephant's brain?
- f. Use your prediction equation to predict the brain weight of an Asian Elephant. The average Asian Elephant weighs 2,547 pounds.
- g. The actual average brain weight of an Asian Elephant is 4,603 grams. How does your prediction compare to the actual average weight of an Asian Elephant's brain?

*\*This problem is adapted from an Illustrative Mathematics task. (<http://www.illustrativemathematics.org/illustrations/1520>)*

## Section 6.1: Construct and Interpret Scatter Plots for Bivariate Data

**Section Overview:** In this section we continue our study of bivariate data, specifically quantitative or numerical data. In 7<sup>th</sup> grade students engaged in the study of univariate data. We begin this section with a problem that deals with univariate data and then use the same context to explore a bivariate data set. As in the case of univariate data, analysis of bivariate measurement data graphed on a scatterplot proceeds by describing shape, center, and spread. Later, we are introduced to Izumi and her basketball statistics and use her data throughout the chapter to build upon the concepts of analyzing bivariate data. In the section students merely learn how to construct, read, and interpret a scatter plot. Throughout this section students investigate and describe trends and patterns of association between two variables and interpret these associations in a variety of real-world situations.

### Concepts and Skills to be mastered:

*By the end of this section students should be able to:*

1. Understand the similarities and differences between univariate and bivariate data.
2. Read and interpret a scatter plot.
3. Construct a scatter plot for bivariate data.
4. Determine whether a scatter plot exhibits a linear, nonlinear, or no apparent association.
5. Describe whether a linear relationship exhibits a positive or negative association.
6. Justify whether an association is weak or strong.
7. Find and analyze clusters and outliers on a scatter plot.



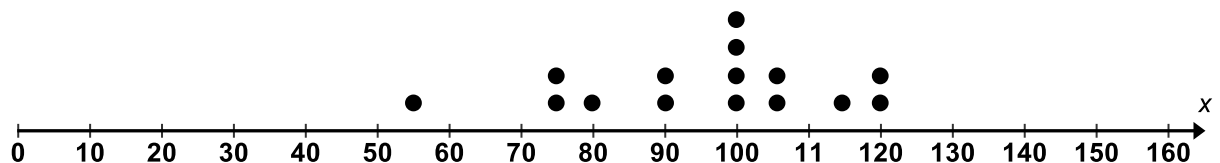
These practice standards are central to this entire section and chapter.

### 6.1a Class Activity: Interpret a Scatter Plot

1. Jenny is a hair stylist. She decides to record the amount of money she makes in tips over a 15-day period. She records the following data:

Day	Amount of Money Made in Tips (dollars)
1	120
2	75
3	80
4	100
5	115
6	100
7	55
8	90
9	100
10	120
11	90
12	105
13	105
14	75
15	100

To better visualize the data, Jenny makes a dot plot of the data.

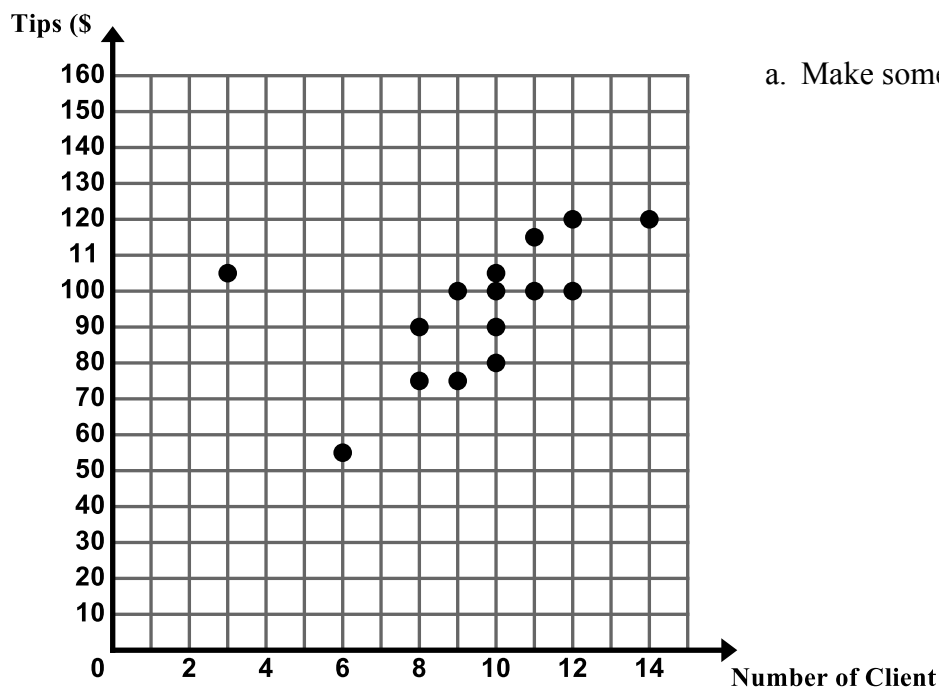


- a. Make some observations about the data shown in the dot plot.

2. Jenny then asks herself the following question: “I wonder if the amount I make in tips is associated to the number of clients I have each day?” She looks back through her appointment book and records the number of clients she had on each of the 15 days. She records the following data.

Day	Number of Clients	Amount of Money Made in Tips (dollars)
1	12	120
2	8	75
3	10	80
4	12	100
5	11	115
6	9	100
7	6	55
8	8	90
9	10	100
10	14	120
11	10	90
12	10	105
13	3	105
14	9	75
15	11	100

To better visualize the data, Jenny makes a **scatter plot** of the data. A **scatter plot** is a graph in the coordinate plane of the set of all  $(x,y)$  ordered pairs of bivariate data.



- a. Make some observations about the scatter plot.



**Directions:** Determine if the following scenarios represent univariate or bivariate data.

3. Lucas conducts an experiment where he records the number of speeding tickets issued in Iron County in a given year along with the average price of gasoline for that same given year. He collects this data from the year 1972 through 2012.
4. Lea conducts an experiment where she records the heights of all the NBA basketball players on the Miami Heat's roster for the 2014 season.
5. Adel conducts an experiment where she records the selling price of several homes in a neighborhood
6. Adel conducts an experiment where she records the selling price and square footage of homes in a neighborhood
7. Lisa conducts an experiment on the number of times a person works out a week and the person's weight

In this chapter, we will focus our study on **bivariate data sets** and we will explore the relationship between two variables of interest.

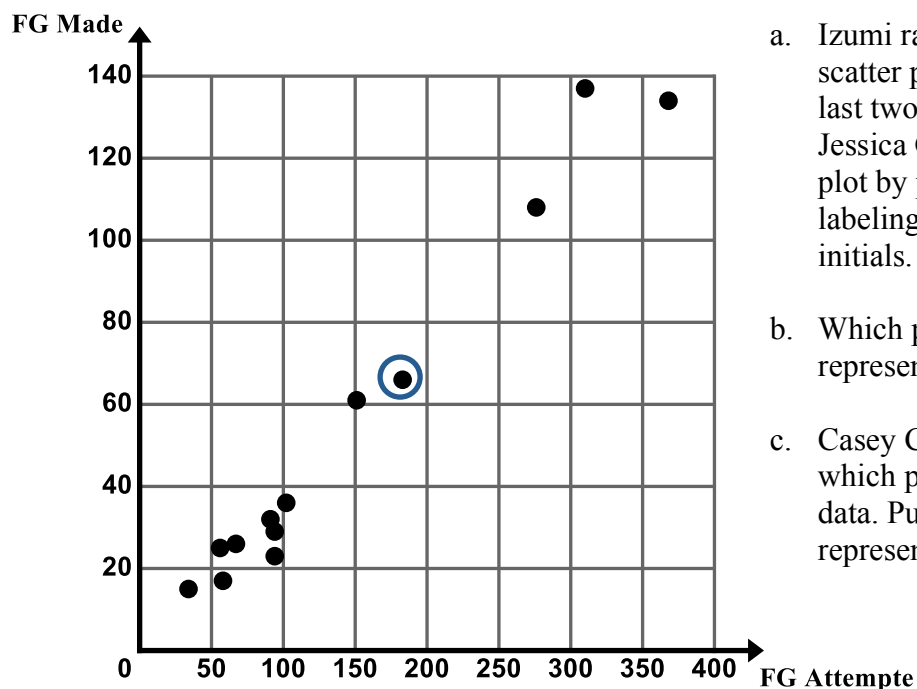
Izumi is the score keeper for her school's basketball team. Izumi's responsibilities as score keeper are to keep a record for several plays during the 2012-2013 season. The basketball plays are listed below.

- Total number of field goals made.  
*In basketball a field goal is the result of the player successfully shooting the basketball through the hoop, regardless of whether it is a two point shot or a three point shot. This does not include foul shots.*
- The total number of field goals attempted.  
*A field goals attempt results when a player tries to make a field goal, an attempt is made whether or not the ball goes through the hoop.*
- The total number of assists.  
*An assist results when the player passes the ball to a teammate who then scores.*
- The total number of rebounds  
*A rebound results when the player retrieves the ball from an unsuccessful field goal attempt.*

The table given below shows the record that Izumi made regarding the number of field goals attempted and the number of field goals made.

Player	Field Goals Attempted	Field Goals Made
Amber Carlson	34	15
Casey Corbin	368	134
Joan O'Connell	94	23
Monique Ortiz	102	36
Maria Ferney	91	32
Amelia Krebs	310	137
Tonya Smith	56	25
Juanita Martinez	58	17
Sara Garcia	151	61
Alicia Mortenson	67	26
Parker Christiansen	94	29
Rachel Reagan	183	66
Paula Lyons	276	108
Thao Ho	221	94
Jessica Geffen	127	54

8. As Izumi examines the data she wonders, “Is there is an association between the number of field goals made and the number of field goals attempted?” To further investigate the relationship between these two random variables, “Field Goals Made” and “Field Goals Attempted” Izumi makes a **scatter plot** of the data as shown below.



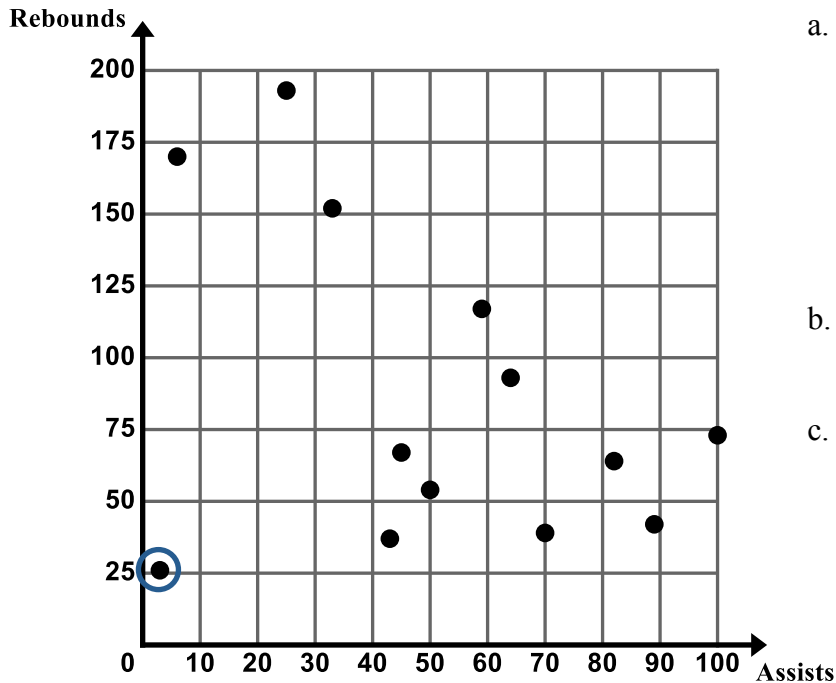
- Izumi ran out of time while creating her scatter plot and did not plot the data for the last two players in the table, Thao Ho and Jessica Geffen. Help Izumi finish the scatter plot by plotting the data for these players and labeling the points with these players' initials.
- Which player does the circled data point represent?
- Casey Corbin sees Izumi's graph and asks which point on the scatter plot represents her data. Put Casey's initials by the point that represents his data.

- d. Using the scatter plot, determine if there is a relationship between field goals attempted and field goals made. Describe any trends or patterns you observe in the data.

9. In addition to data about field goals, Izumi is curious about the relationship between the number of assists and the number of rebounds a player makes in a season. In order to study this relationship, Izumi gathers data on the number of assists and rebounds each player makes during the season. Izumi's Assist and Rebound data are given in the following table.

Player	Assists	Rebounds
Amber Carlson	82	64
Casey Corbin	6	170
Joan O'Connell	43	37
Monique Ortiz	50	54
Maria Ferney	89	42
Amelia Krebs	25	193
Tonya Smith	70	39
Juanita Martinez	3	26
Sara Garcia	100	73
Alicia Mortenson	33	152
Parker Christiansen	64	93
Rachel Reagan	45	67
Paula Lyons	59	117
Thao Ho	15	179
Jessica Geffen	30	113

Izumi made the scatter plot of assists vs. rebounds shown below to help her better visualize the data.



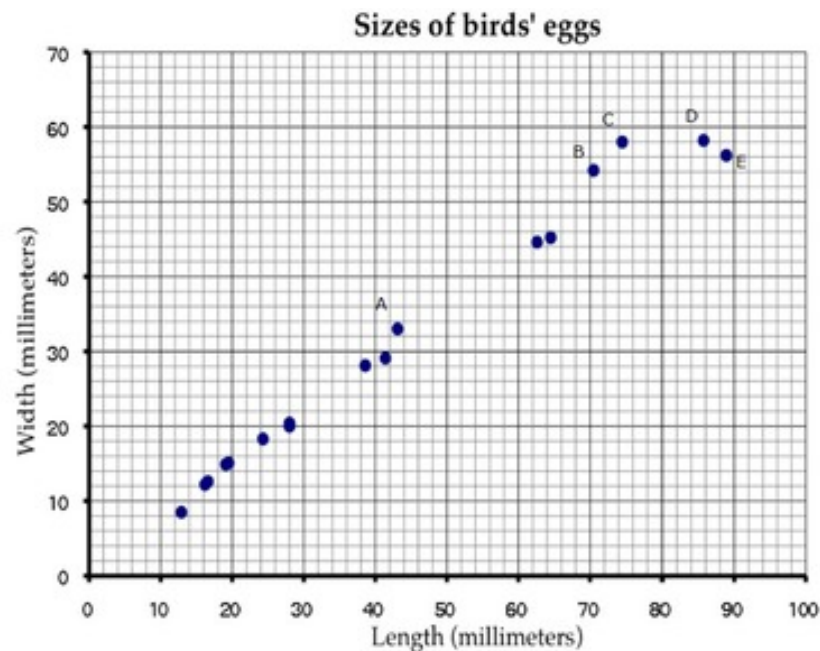
- Again, Izumi ran out of time while creating her scatter plot and did not plot the data for the last two players in the table, Thao Ho and Jessica Geffen. Help Izumi finish the scatter plot by plotting the data for these players and labeling the points with these players' initials.
- Which player does the circled data point represent?
- Locate the data points for 3 different players and put the initials of the players next to their data point.

- Izumi notices the circled data point stands out noticeably from the general behavior of the data set. We call this point an **outlier**. Give some plausible reasons as to why this player's data does not fit with the rest of the data.
- Using the scatter plot, determine if there is a relationship between number of assists and number of rebounds. Describe any trends or patterns you observe in the data.

10. Which data set appears to have a stronger association: number of field goal made vs. number of field goal attempts or number of rebounds vs. number of assists?

### 6.1a Homework: Interpret a Scatter Plot

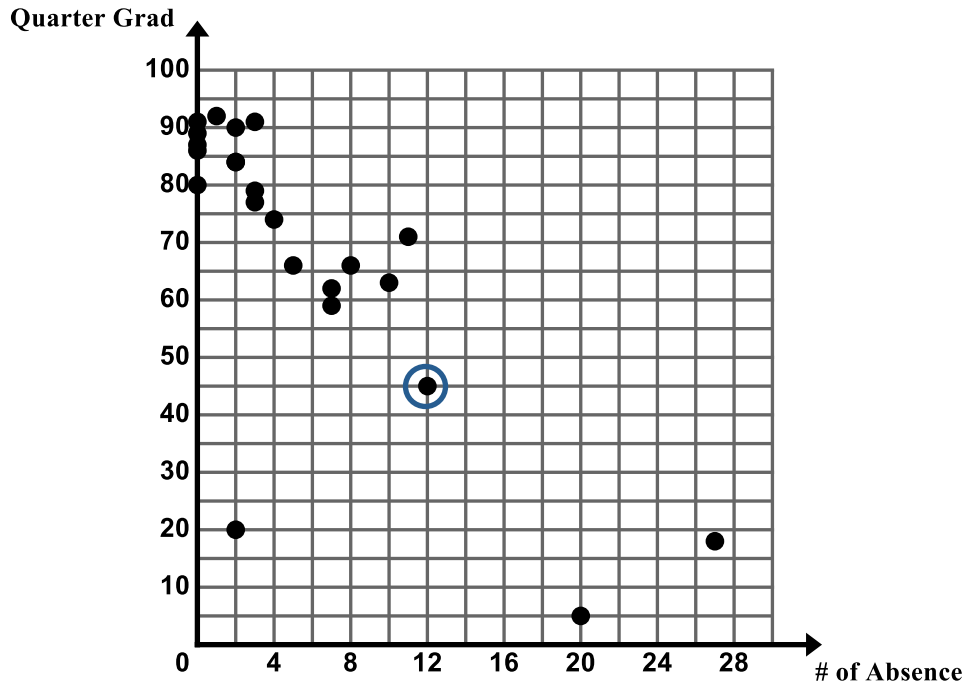
1. This scatter diagram shows the lengths and widths of the eggs of some American birds.



- A biologist measured a sample of one hundred Mallard duck eggs and found they had an average length of 57.8 millimeters and average width of 41.6 millimeters. Use an X to mark a point that represents this on the scatter diagram.
- What does the graph show about the relationship between the lengths of birds' eggs and their widths?
- Another sample of eggs from similar birds has an average length of 35 millimeters. If these bird eggs follow the trend in the scatter plot, about what width would you expect these eggs to have, on average?
- Describe the differences in shape of the two eggs corresponding to the data points marked C and D in the plot.
- Which of the eggs A, B, C, D, and E has the greatest ratio of length to width? Explain how you decided.

*Note: This is an Illustrative Mathematics Task (<http://www.illustrativemathematics.org/illustrations/41>)*

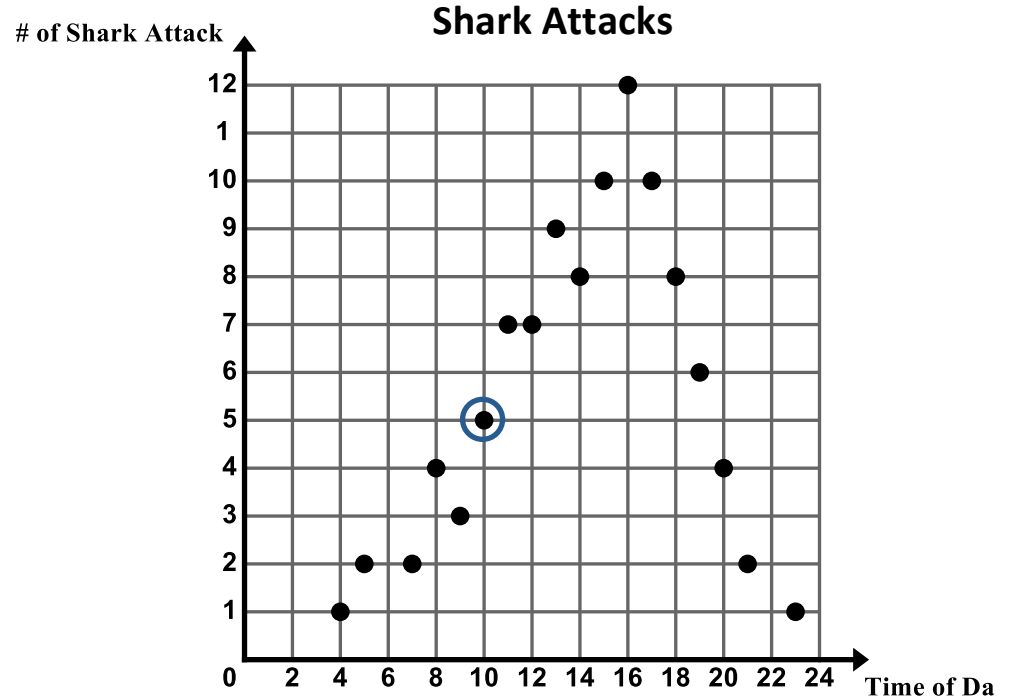
2. Ms. Ganchero is a math teacher. She wonders if there is an association between the number of absences a student has in her class and the grade they earn at the end of the quarter. In order to analyze this relationship, Ms. Ganchero created the scatter plot below which shows the number of absences a student has in a quarter and their final grade at the end of the quarter.



- While reviewing the scatter plot, Ms. Ganchero realized that she did not plot the data for two students. Rachel was absent 5 times and received a final grade of 72 and Lydia was absent 10 times and received a final grade of 55. Plot and label these two data points on the scatter plot above.
- What does the circled data point represent in the context?
- Give a plausible reason for the cluster of points in the upper left corner of the graph.
- Do there appear to be any outliers in the data? If yes, what are they? Give a plausible reason for the outlier(s).
- Does the scatter plot suggest a strong relationship between absences and grade? Describe any trends or patterns you observe in the data.

3. A long stretch of a popular beach is overseen by the local coast guard. Over a period of 60 years the coast guard has kept track of the number of shark attacks occurring along the coast as well as the hour during the day in which the attack occurred. The table and corresponding scatter plot show this data. **\*Note:** The time of day is given by a 24 hour clock, also known as military time.

Hour during the day	Number of Shark Attacks
04:00	1
05:00	2
07:00	2
08:00	4
09:00	3
10:00	5
11:00	7
12:00	7
13:00	9
14:00	8
15:00	10
16:00	12
17:00	10
18:00	8
19:00	6
20:00	4
21:00	2
23:00	1



- What does the circled data point represent in the context?
- Describe the association that exists between the time of day and the number of shark attacks. Give a possible explanation as to why this graph is shaped the way it is.

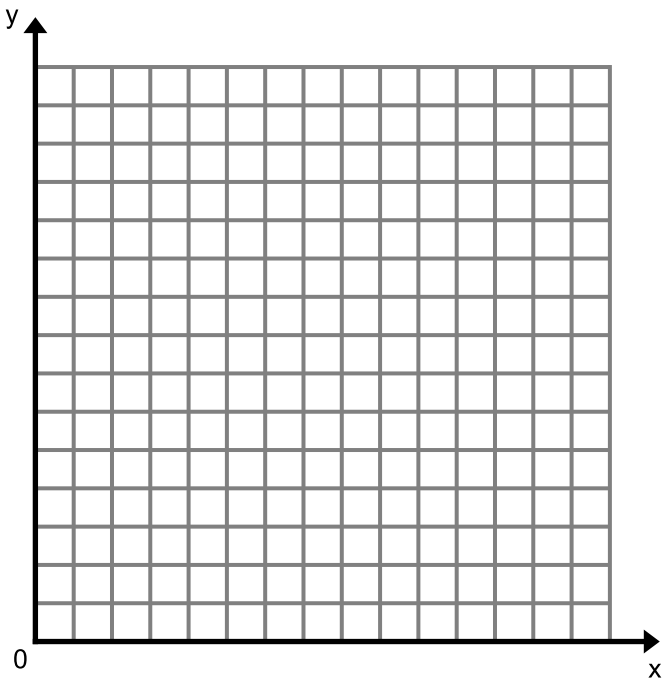
For tomorrow's class, you will need data on the height and shoe size of 5 people. Be sure to gather this data from different aged people – younger siblings, older siblings, parents, grandparents. Record your data here for tomorrow's class.

6.1b Class Activity: Create and Analyze a Scatter Plot

- 1. Do you anticipate an association between a person’s height and their shoe size?
  - a. Make a prediction.
  - b. Collect your class data in the table below.

	Height	Shoe Size
1.		
2.		
3.		
4.		
5.		
6.		
7.		
8.		
9.		
10.		
11.		
12.		
13.		
14.		
15.		

- c. Make a scatter plot of the data.



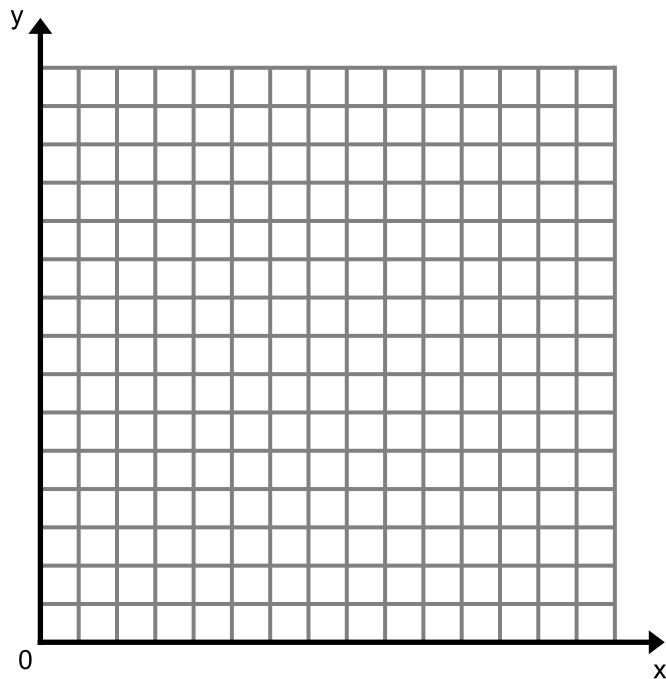
- d. Using the scatter plot, determine if there is an association between a person’s shoe size and height. Describe any trends or patterns you observe in the data including clusters and outliers.



2. Is there an association between the number of letters in a person's first name and the number of letters in a person's last name?
  - a. Make a prediction.
  - b. Collect your class data in the table below.

Person's first and last name	Number of letters in their first name	Number of letters in their last name

- c. Make a scatter plot of the data.



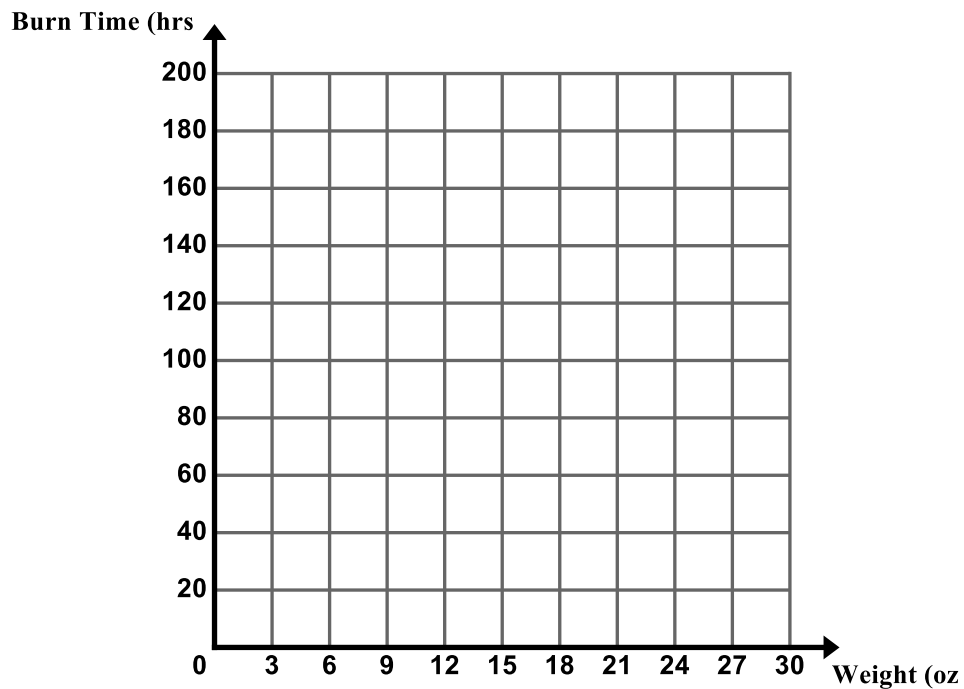
- d. Using the scatter plot, determine if there is an association between the number of letters in a person's first name and the number of letters in their last name. Describe any trends or patterns you observe in the data including clusters and outliers.

## 6.1b Homework: Create and Analyze a Scatter Plot

1. Is there an association between the weight of a candle and the amount of time it burns?
  - a. Make a prediction.
  - b. A company that manufactures candles tests the amount of time it takes for several candles of several different weights to burn. The results are shown in the table below.

Candle Weight (ounces)	2	2	2	3	3	4	4	5	5	5	10	10	10	16	16	16	22	22	22	26	26
Burn Time (hours)	15	16	18	20	33	34	35	38	40	36	40	80	80	95	100	98	120	125	175	174	180

- c. Make a scatter plot of the data on the graph provided.



- d. Using the scatter plot, determine if there is an association between the weight of a candle and how long it burns. Describe any trends or patterns you observe in the data including clusters and outliers.

### 6.1c Classwork: Patterns of Association

So far in our study of bivariate data, we have seen data sets that show different **types of association** between two variables. There are many ways that we can describe the association (if there is one) between two variables. Common ways to talk about the association of two variables are shown in the table below. **Sketch scatter plots that correspond to each of the four associations described.**

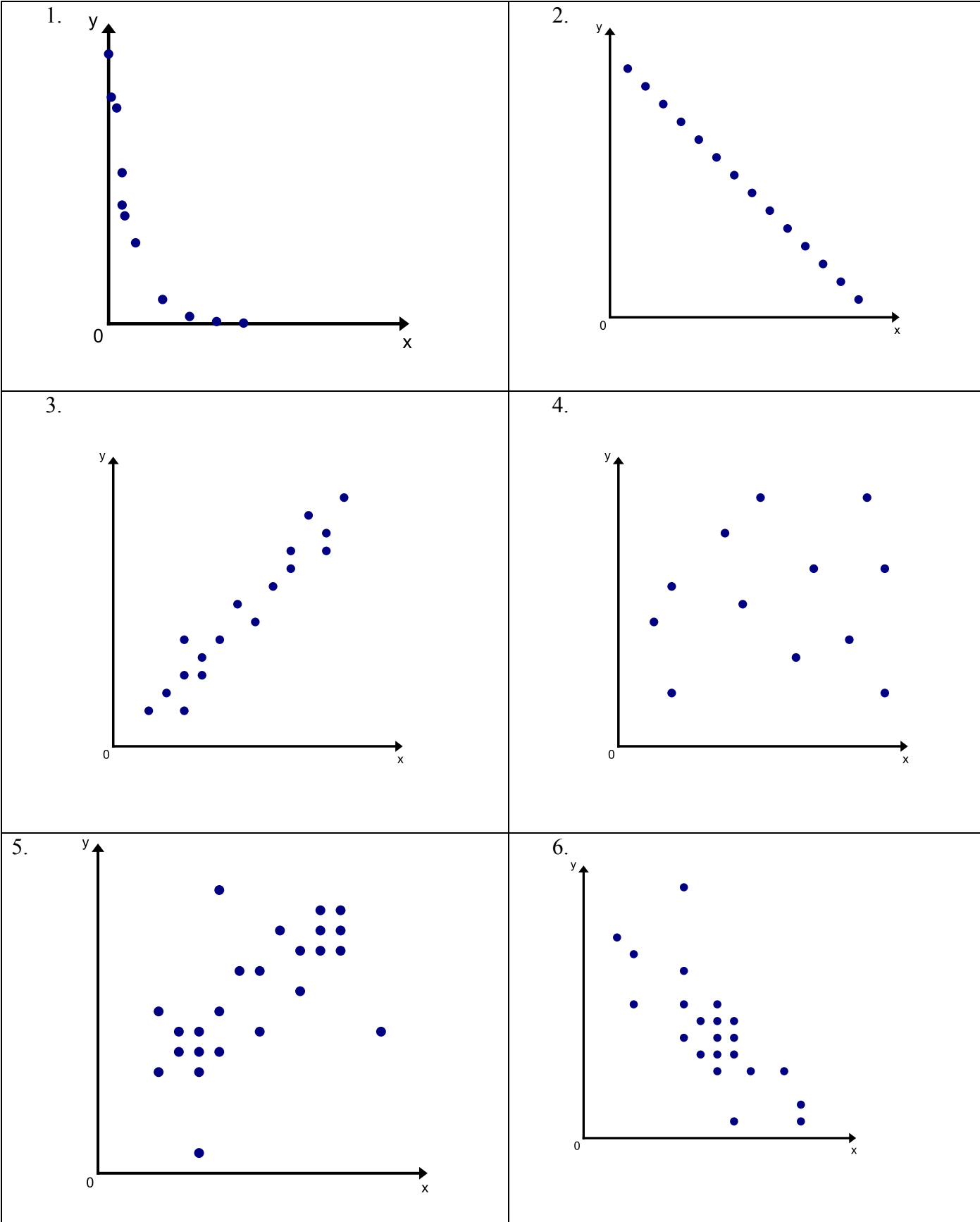
1. <b>Positive Linear Association</b>	2. <b>Negative Linear Association</b>
3. <b>No Apparent Association</b>	4. <b>Nonlinear Association</b>

If the variables show a linear association, we can determine whether that relationship is **strong**, **weak**, or **perfect**. Imagine drawing a line through the center of the points—EYEBALLING the line. If the data points are closely packed around your line, the linear relationship is a **strong** one. If the data points are more spread out from the line, the linear relationship is a **weak** one. If your data points fall on a straight line, the linear association is **perfect**.

We may also observe the following patterns in our data:

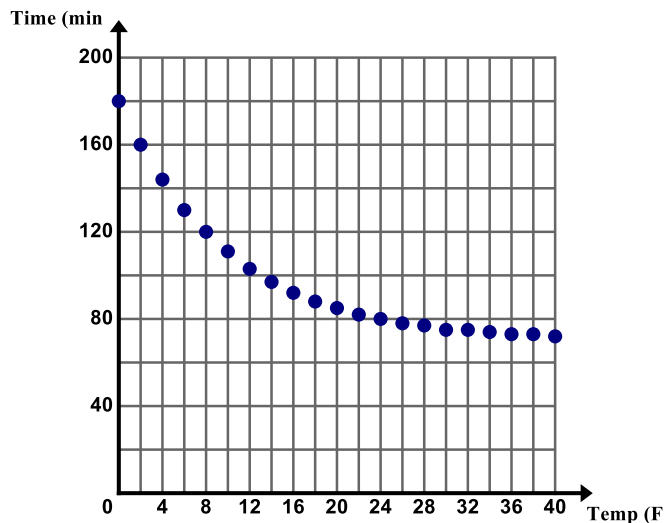
- **Clusters** - A cluster is a set of points that are in close proximity to each other.
- **Outliers** - An outlier is a data point that noticeably stands out from the general behavior of the data set.

**Directions:** Describe the association between  $x$  and  $y$  using the terms above. Circle any clusters in the data. Put a star by any points that appear to be outliers.



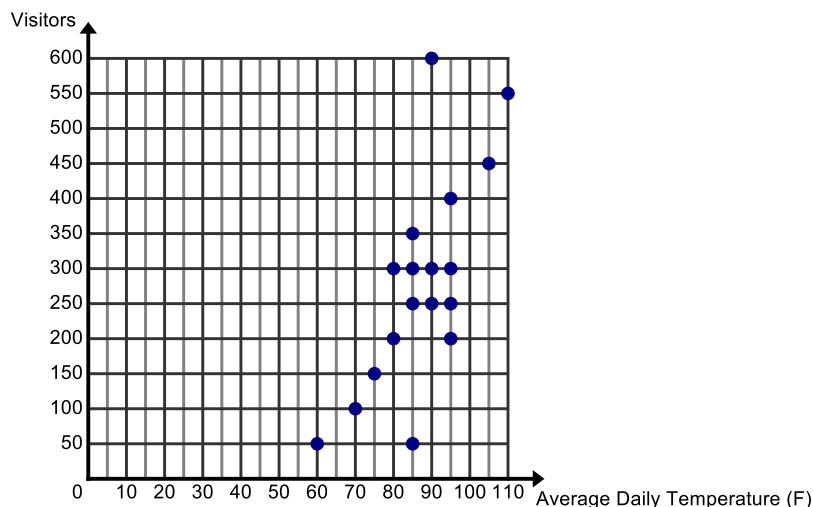
**Directions:** Examine the following scatter plots. Describe the association between the two variables. Circle any clusters in the data. Put a star by any points that appear to be outliers. Use the context to give possible explanations as to why these trends, patterns, and associations exist.

7. The scatter plot given below shows the temperature of a cup of tea sitting on the counter for 30 minutes. The cup of tea is sitting in a room that is 70 degrees.

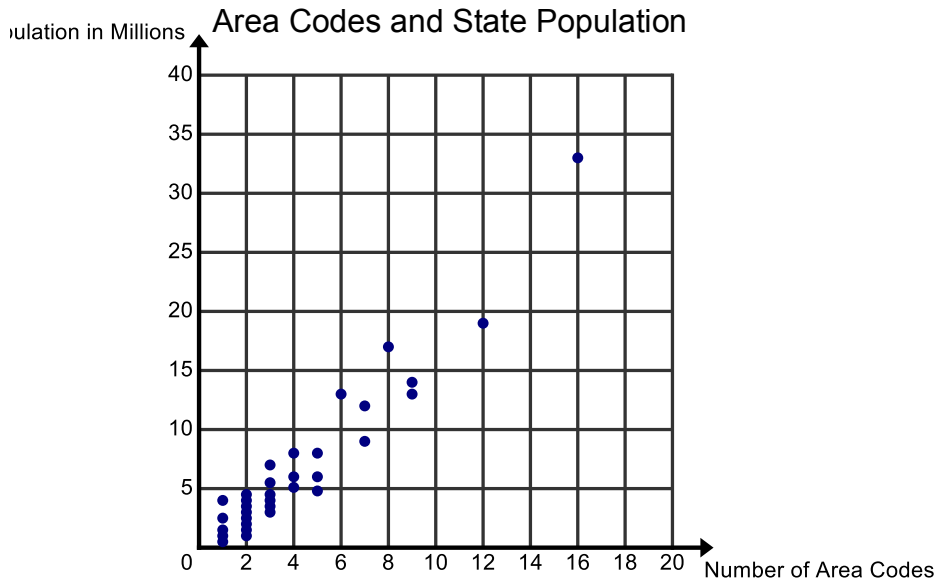


8. The Paradise Pool records the average daily temperature and the number of visitors to their pool for 18 days throughout the month of July. On July 24<sup>th</sup>, to celebrate Pioneer Day, admission is half off. The average daily temperature on that day is 90 degrees.

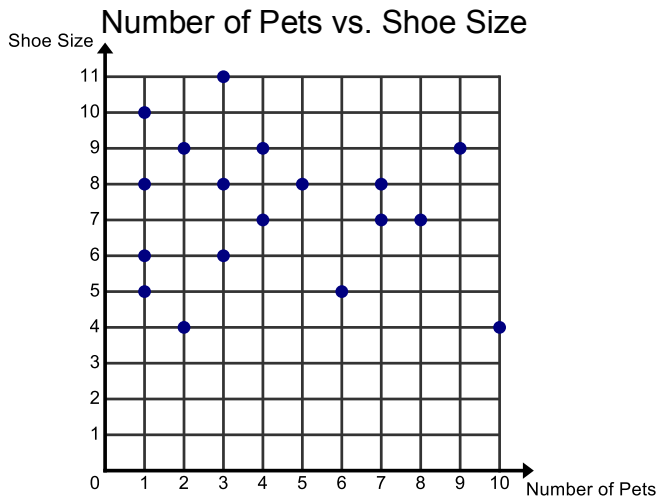
Temperature vs. Visitors at a Swimming Pool



9. The number of Area Codes versus a state's population is shown in the plot below.



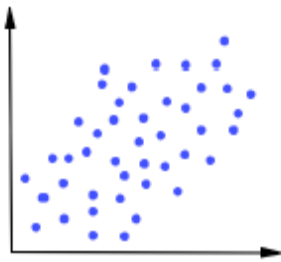
10. Holly's math teacher asks her to conduct her own survey to study different types of association. She chooses to investigate the number of pets a person has verses their shoe size.



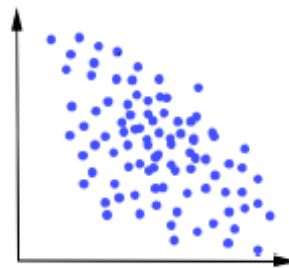
### 6.1c Homework: Patterns of Association

**Directions:** Describe the association between  $x$  and  $y$ . Circle any clusters in the data. Put a star by any points that appear to be outliers.

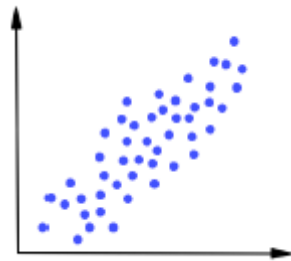
1.



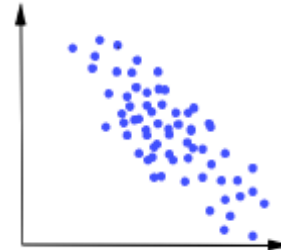
2.



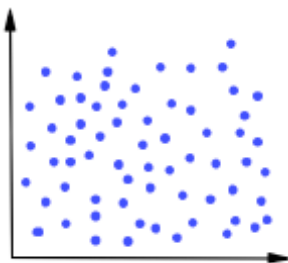
3.



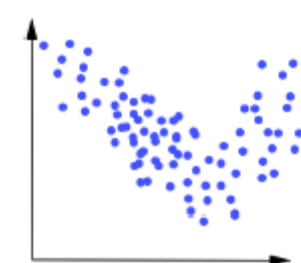
4.



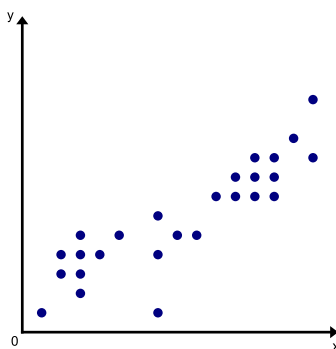
5.



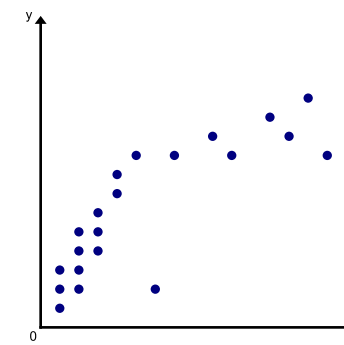
6.



7.



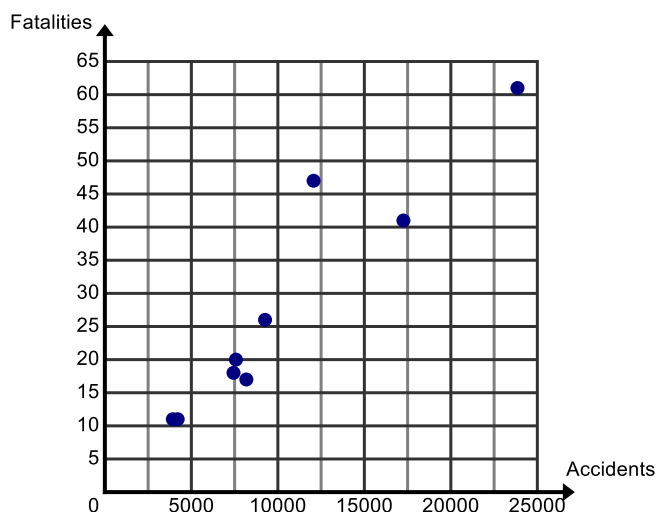
8.



**Directions:** Examine the following scatter plots. Describe the association between the two variables. Circle any clusters in the data. Put a star by any points that appear to be outliers. Use the context to give possible explanations as to why these trends, patterns, and associations exist.

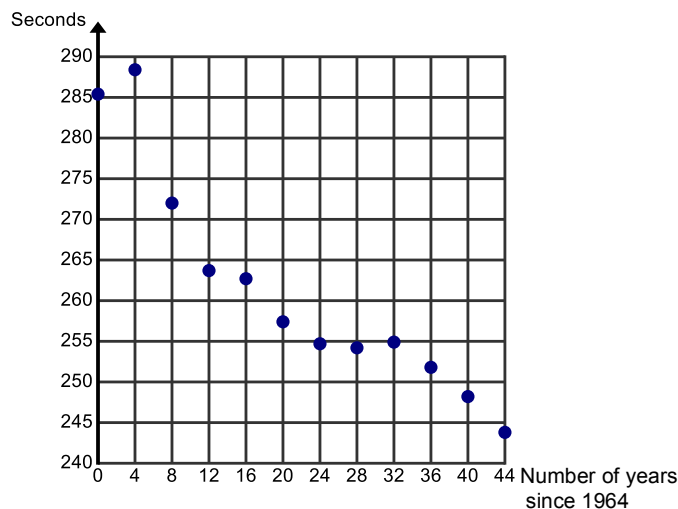
9. For Heidi's Driver's Education class, she finds data about the number of car accidents and fatalities (deaths) from car accidents for teens in the Western United States.

Accidents vs. Fatalities for Teen Drivers in 2006 in the Western United States



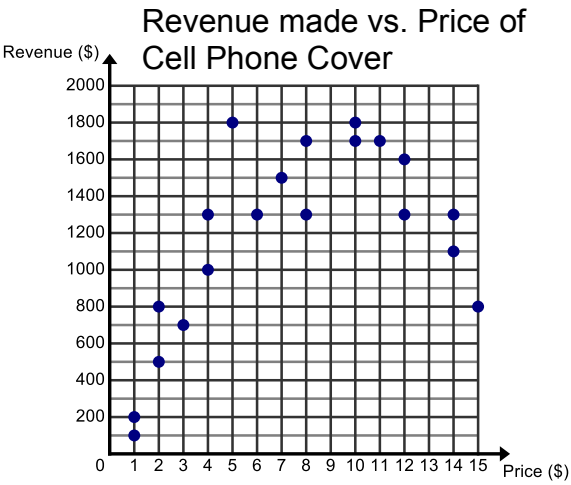
10. Winning times for the Individual Swimming Medley in the Olympics from 1964-2008 are in the plot below. Michael Phelps' times are the last two entries.

400-Meter Individual Swimming Medley in Olympics (1964 – 2008)





11. Hannah has a kiosk in the mall where she is selling Cell Phone Covers. She records how much money she makes (revenue) in relationship to the price she charges for the covers.



## 6.1d Self-Assessment: Section 6.1

Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept.

Skill/Concept	Beginning Understanding	Developing Skill and Understanding	Deep Understanding, Skill Mastery
1. Understand the similarities and differences between univariate and bivariate data.			
2. Read and interpret a scatter plot.			
3. Construct a scatter plot for bivariate data.			
4. Determine whether a scatter plot exhibits a linear, nonlinear, or no apparent association.			
5. Describe whether a linear relationship exhibits a positive or negative association.			
6. Justify whether an association is weak or strong.			
7. Find and analyze clusters and outliers on a scatter plot.			

How did you use the following practice standards in this section?



## Section 6.2 Use a Linear Model to Solve Problems

### Section Overview:

In this section, students continue to construct and interpret scatter plots. For scatter plots that suggest a linear association, students informally fit a straight line to the data and informally assess the model fit by judging the closeness of the data points to the line. They also analyze how outliers affect a line of best fit and reason about whether to drop outliers from a data set. They begin to make predictions using the line of best fit and briefly see how an equation can be used to make predictions about data as well, noting that limitations exist for analyzing data for extreme values of  $x$ . As they write their equations they begin to interpret the slope and  $y$ -intercept of their linear models. This is where important information can be gleaned from the statistical data and meaningful predictions can be made. As students continue to analyze linear models they use their equations to make predictions about the data, keeping in mind that most statistical data has its limitations. Throughout the section they must use a critical eye and exploit their knowledge about the subject matter the linear model illustrates as they analyze the data.

### Concepts and Skills to be mastered:

*By the end of this section students should be able to:*

1. Know that a line of best fit is a linear model that shows the relationship between two variables.
2. Draw a line of best fit for linear models.
3. Determine how outliers affect a line of best fit.
4. Informally assess the model fit by judging the closeness of the data points to the line.
5. Write an equation for the line of best fit.
6. Explain the meaning of the slope and  $y$ -intercept in context.
7. Use the equation of a linear model to solve problems.



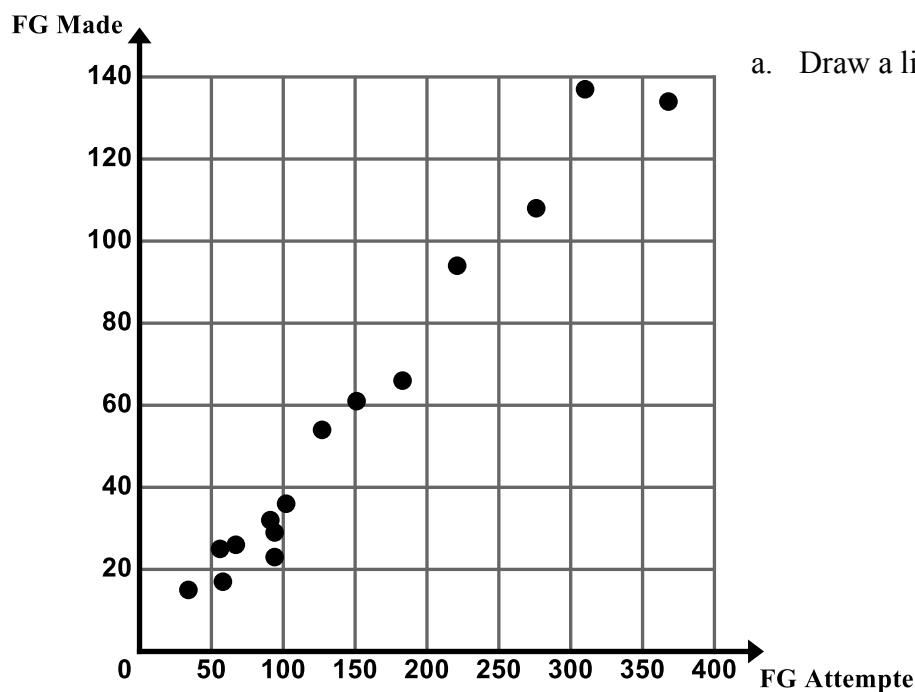
These practice standards are central to this entire section and chapter.

## 6.2a Class Activity: Fit a Linear Model to Bivariate Data

Most real-world data does not fall perfectly on a line. However, if the data on a scatter plot resembles a line, we can fit a line to the data, write an equation for the line, and use this equation to solve problems and make predictions.

The line that you use to represent the data is called **the line of best fit**. The function you write for the line of best fit is the **prediction function**. The most common way to find the line of best fit is to use the “eye-balling” technique. Simply try to draw a straight line that best fits the data. Let’s revisit some examples from section 1 where the two variables of interest had a linear association and determine a line of best fit for the data.

1. Once again refer back to Izumi’s basketball statistics. Look at the scatter plot for Field Goals Made vs. Field Goals Attempted.



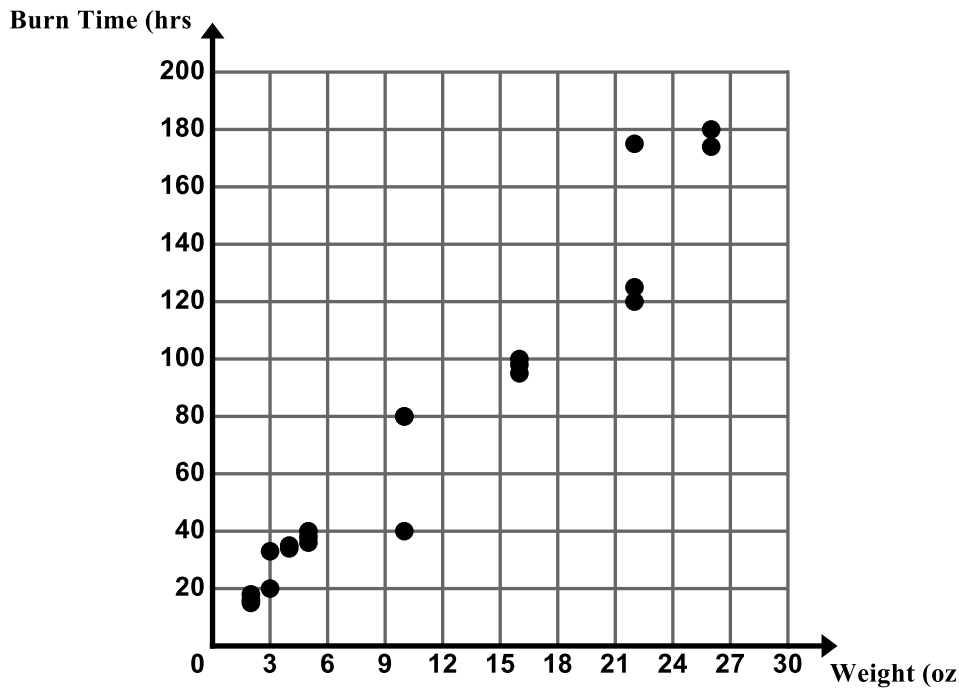
- a. Draw a line of best fit on the scatter plot.

- b. Write an equation for the line of best fit you drew.

- c. Explain the meaning of the slope and  $y$ -intercept in the context.
  
  
  
  
  
  
  
  
  
  
- d. Use your prediction equation to predict the number of field goals a person would make if they attempted 500 field goals.
  
  
  
  
  
  
  
  
  
  
- e. Use your prediction equation line of best fit to predict the number of field goals a person would make if they attempted 102 field goals.
  
  
  
  
  
  
  
  
  
  
- f. Is the association between number of field goals attempted and number of field goals made strong or weak? Justify your answer.

2. The following scatter plot shows the burn time for candles of various weights.

a. Draw a line of best fit on the scatter plot.



b. Write an equation for the line of best fit you drew.

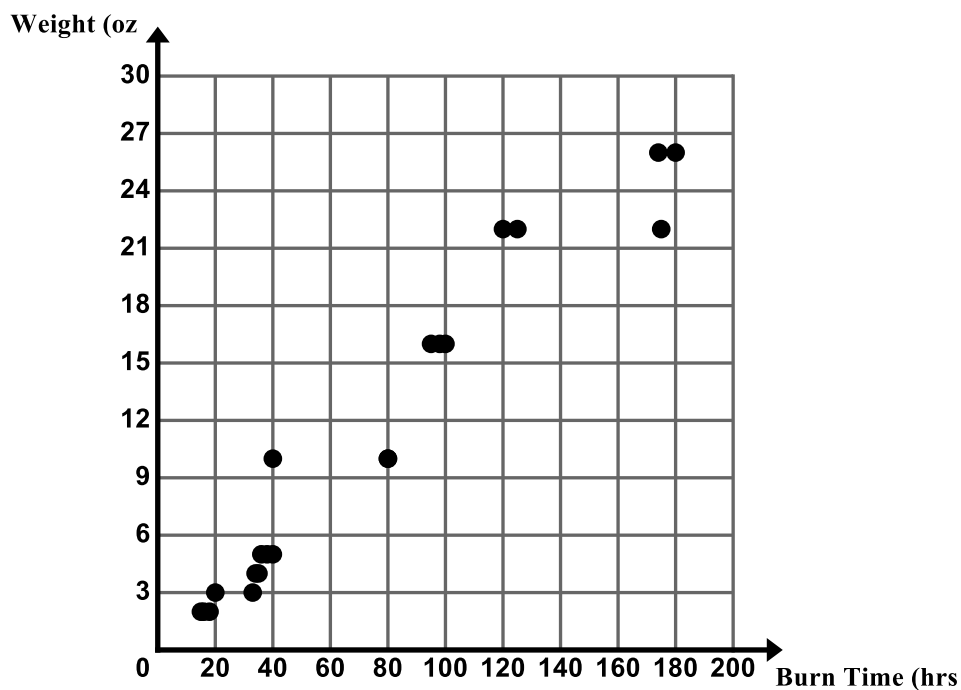
c. Explain the meaning of the slope and y-intercept in the context.

d. Use your prediction equation to predict the burn time for a candle that weighs 40 ounces.

e. If candle burns out at 500 hours, predict how much the candle weighs.

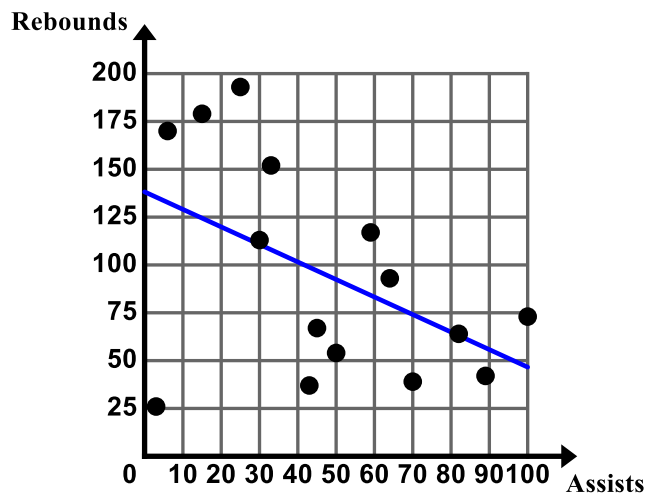
f. What do you think would happen if we changed the graph above so that burn time was on the  $x$ -axis and weight was on the  $y$ -axis? Would our data still resemble a line? What would happen to the slope and  $y$ -intercept of the line of best fit?

3. The following scatter plot shows the burn time for candles of various weights. This time, burn time has been graphed on the  $x$ -axis and weight has been graphed on the  $y$ -axis.



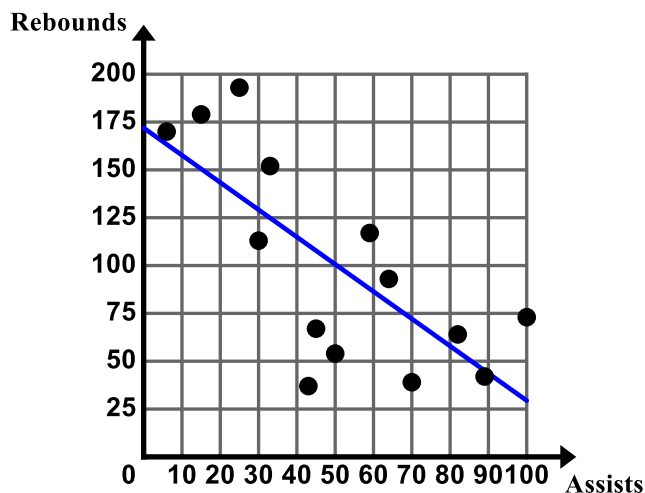
- Was your prediction on the previous page correct?
  - Draw a line of best fit on the scatter plot.
  - Write an equation for the line of best fit you drew.
- d. How does this new equation compare to your equation in #2? What accounts for this change?

4. Software programs and graphing calculators can be used to draw lines of best fit. Izumi used a graphing calculator to generate a line of best fit for her data on assists and rebounds. The graph below shows the line of best fit generated by the calculator.



- a. After creating this line of best fit, Izumi decided that it might be best to drop the outlier (3, 26) from her data set. Is it reasonable for Izumi to drop the outlier from her data set? Why or why not?

After dropping the outlier, Izumi used the calculator to generate a new line of best fit.



- b. Analyze the differences in the two lines. What did the outlier do to the line of best fit generated by the calculator?
- c. Write a prediction equation for the line of best fit generated by the calculator with the data set that does **not** include the outlier.

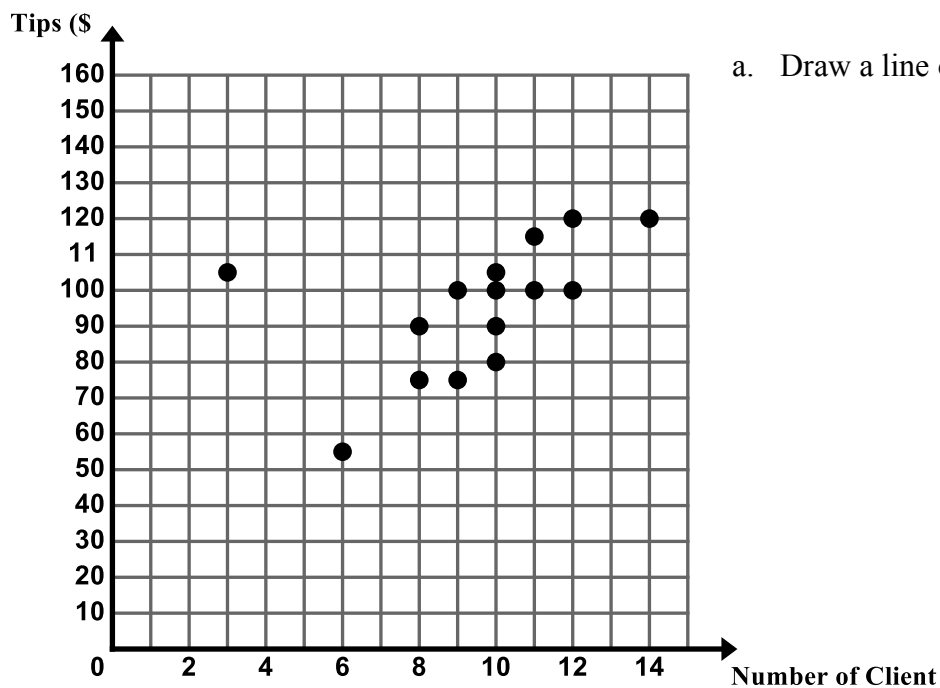


- d. Explain the meaning of the slope and  $y$ -intercept in the context.
  
  
  
  
  
  
  
  
  
  
- e. Use your function to predict the number of rebounds a random player would have if they made 110 assists throughout the season? 150 assists? Explain the limitations that the data exhibits.
  
  
  
  
  
  
  
  
  
  
- f. Similarly use your function to predict the number of assists a random player would have if they made 150 rebounds throughout the season.
  
  
  
  
  
  
  
  
  
  
- 5. Which scatter plot, the Field Goals Made vs. Field Goals Attempts or Rebounds vs. Assists, is more closely aligned with its line of best fit? Justify your answer. What does this tell us about the strength of each of the associations? What does this tell us about the accuracy of using each of the prediction lines to make predictions?

## 6.2a Homework: Fit a Linear Model to Bivariate Data

**Directions:** For the following problems you will be drawing a line of best fit, writing a prediction equation, and using that equation to make predictions. **Prior to drawing your line of best fit, determine whether you should remove any outliers from your data set.**

1. The following scatter plot shows the amount of money Jenny makes in tips based on how many clients she has in a day.



a. Draw a line of best fit on the scatter plot.

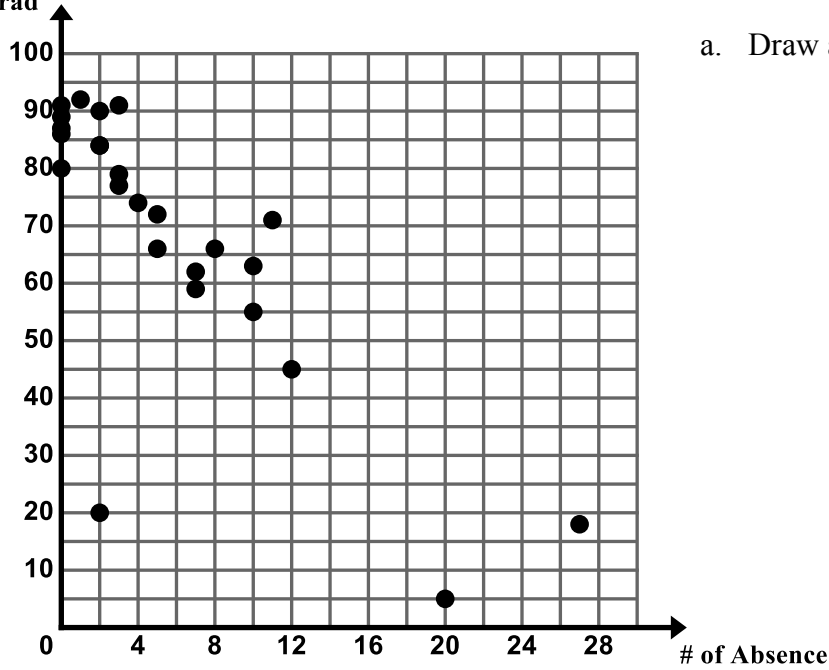
b. Write an equation for the line of best fit you drew.

c. Explain the meaning of the slope and y-intercept in the context.

d. Use your prediction equation to predict the amount Jenny would make in tips if she had 18 clients in one day.

2. The following scatter plot shows the final grade in Ms. Ganchero's math class for students vs. the number of times they are absent.

Quarter Grad



- a. Draw a line of best fit on the scatter plot.

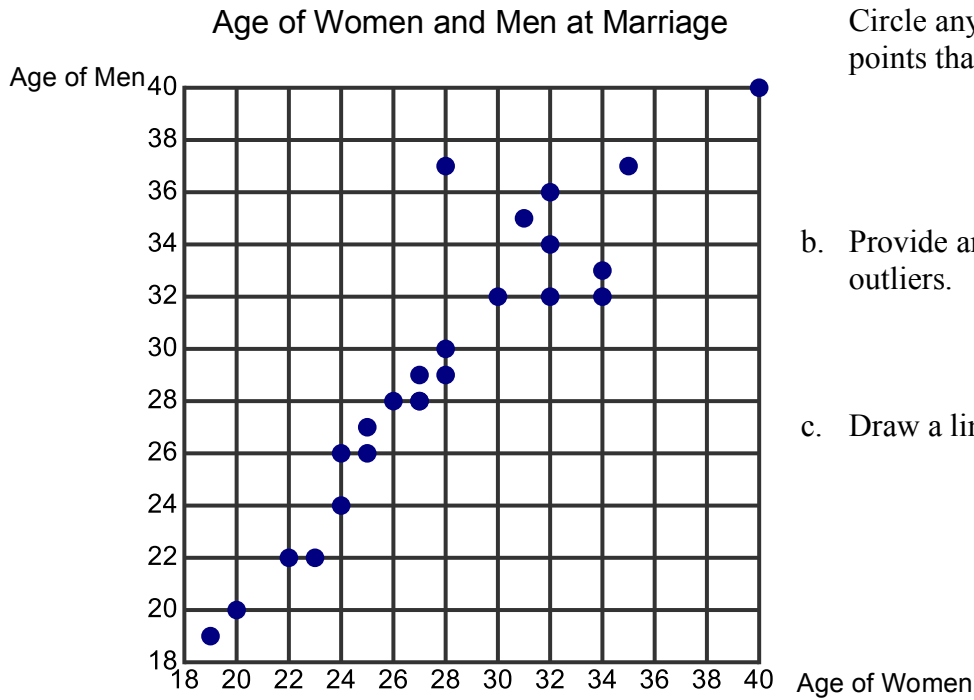
- b. Write an equation for the line of best fit you drew.

- c. Explain the meaning of the slope and y-intercept in the context.

- d. Use your prediction equation to predict the final grade of a student who is absent 16 times.

- e. Use your prediction equation to predict how many times a student is absent who receives a final grade of 5 in the class.

3. Bethany is interested in the relationship between the age of when men and women get married. She surveys 24 couples and asks them the age in which they got married for the first time. A scatter plot of her data is below.



- a. Describe the association between the two variables. Circle any clusters in the data. Put a star by any points that appear to be outliers.

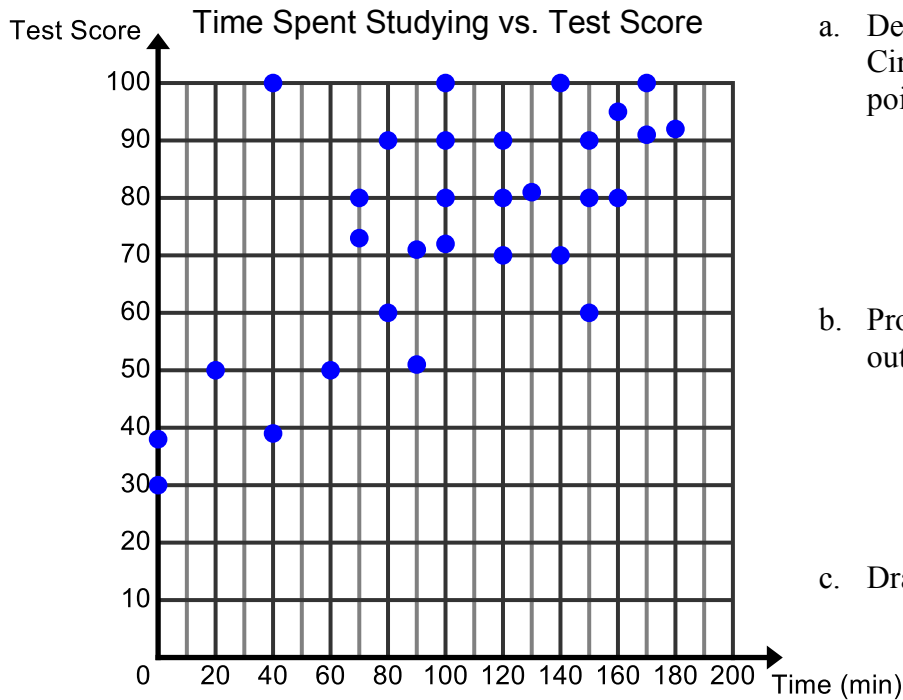
- b. Provide an explanation for any clusters of data or outliers.

- c. Draw a line of best fit on the scatter plot.

- d. Write an equation for the line of best fit you drew.

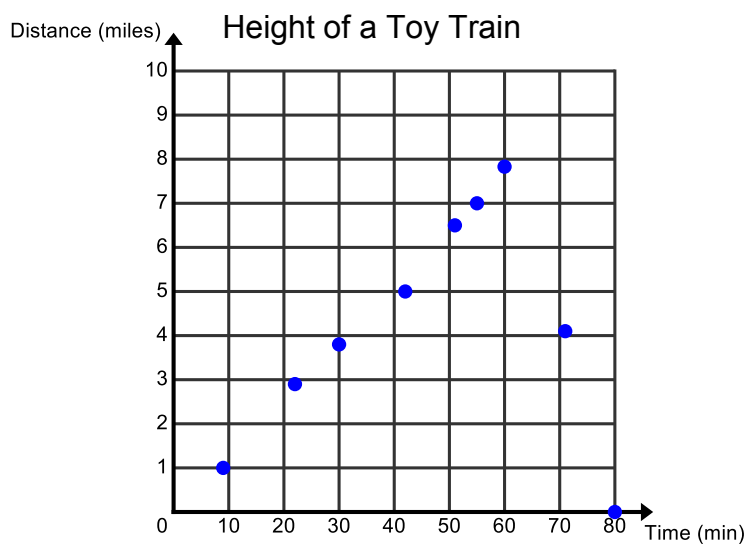
- e. Use your prediction equation to predict the age of a man when he gets married if the woman that he marries is 38.

4. Jenna is interested in the association between the time spent studying for a test and the score that is earned. She surveys 30 people about the time they spent studying for a test and the score that they earned on the test. Her data is in the scatter plot below.



- Describe the association between the two variables. Circle any clusters in the data. Put a star by any points that appear to be outliers.
- Provide an explanation for any clusters of data or outliers.
- Draw a line of best fit on the scatter plot.
- Write an equation for the line of best fit you drew.
- Explain the meaning of the slope and y-intercept of your line of best fit in the context.
- Use your prediction equation to predict the score for a person who studies for 160 minutes.
- Compare and contrast the prediction calculated using the equation with the actual data points of the people who studied for 160 minutes.
- Does the association between these two variables appear to be weak or strong? Provide an explanation regarding why the strength is this way.

5. A scatter plot given below is about the height of a toy train attached to a weather balloon. A GPS (global positioning system) records the height of the toy train about every ten minutes that it is in the air. When the train reaches the stratosphere the weather balloon pops.

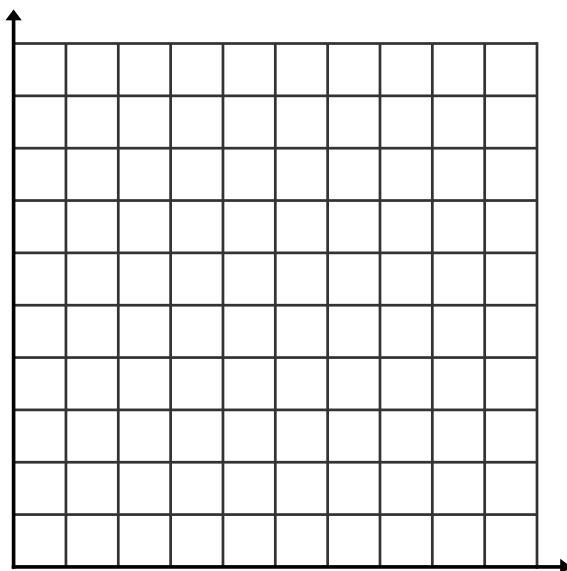


- a. What kind of association exists for this data?
- b. Would it be feasible to draw a line of best fit for this data? Why or why not.

6. The table gives data relating the number of oil changes every two years to the cost of car repairs.

- a. Plot the data on the graph provided, with the number of oil changes on the horizontal axis. You will need to define your own scale.

Oil Changes	3	5	2	3	1	4	6	4	3	2	0	10	7
Repair Costs	\$300	\$300	\$500	\$400	\$700	\$400	\$100	\$250	\$450	\$650	\$600	\$0	\$150



- b. Write a sentence describing the association between the number of oil changes and the cost of car repairs. Is the association weak or strong?
- c. Are there any outliers or clusters that affect the data?
- d. Draw a line of best fit for the data. Assess how well the line fits the data.
- e. What is the slope of the line of best fit and what does it represent?
- f. What is the  $y$ -intercept of the line and what does it represent?

- g. Write an equation in slope-intercept form that you could use to predict the cost of repairs,  $y$ , for any number of oil changes,  $x$ . Compare your prediction with that of a partner.
  
  
  
  
  
  
  
  
  
  
- h. Use your equation to predict how much a person would spend on car repairs if they were to get 8 oil changes. Compare your prediction with that of a partner.
  
  
  
  
  
  
  
  
  
  
- i. If a person spent \$1000 dollars on car repairs how many oil changes would you expect them to have?
  
  
  
  
  
  
  
  
  
  
- j. Based off of this data what would you recommend as the ideal number of oil changes to get every two years.



## 6.2b Class Activity: Tongue Twister

Students will say a selected tongue twister one at a time. In the first trial, only the first student will say the tongue twister; in the second trial, only the first and second students will say the tongue twister, etc. In each trial, one person will be added to the chain of tongue twisters and the total elapsed time will be recorded.

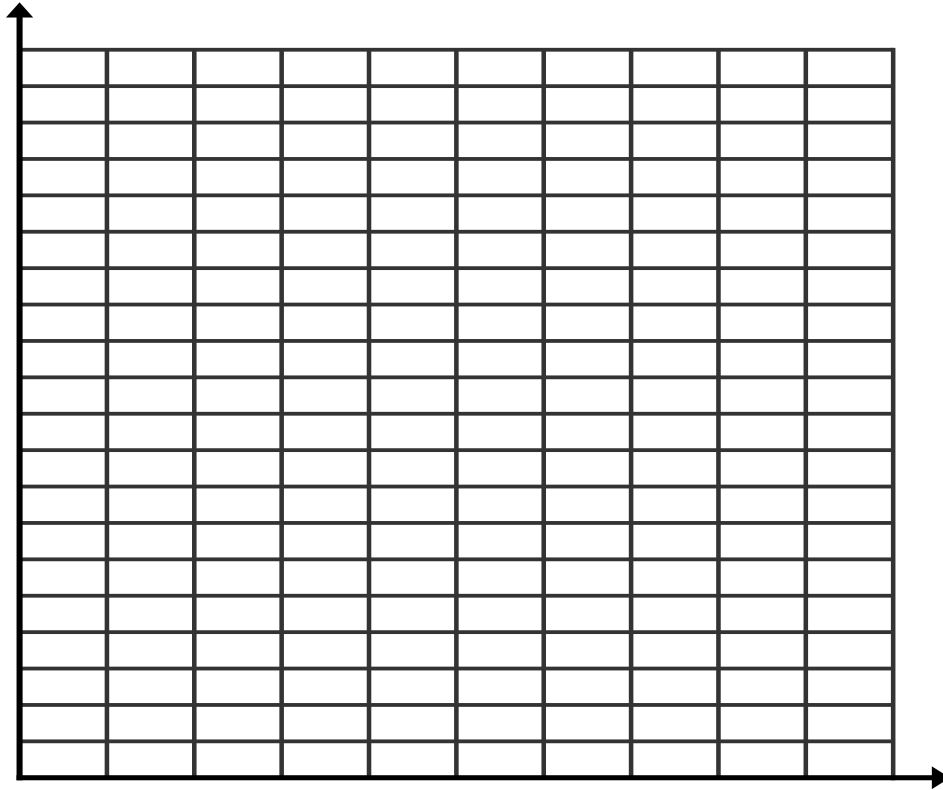
Tongue twisters:

- A. Work will win when wishy-washy wishing won't.
- B. Three witches wished three wishes, but which witch wished which wish.
- C. Peter Piper picked a peck of pickled peppers.
- D. Picky people pick Peter Pan peanut butter it is the only peanut butter picky people pick.

1. In the table below, record the class data for each Tongue Twister.

Number of people	Tongue Twister A (time)	Tongue Twister B (time)	Tongue Twister C (time)	Tongue Twister D (time)
1				
2				
3				
4				
5				
6				
7				
8				
9				

2. Make a scatter plot using different colors for each tongue twister's data. Make sure you label and title the graph.



3. What kind of association exists for this relationship?
4. Draw a line of best fit (in the matching color) for each tongue twister.
5. Even though we did not measure the time required for 18 people to say the tongue twister, explain clearly how you can use the line you drew in #4 to predict this time for just one of the tongue twisters. Similarly, explain clearly how you can use the line to determine how many people could say the tongue twister in 70 seconds.

18 people

70 seconds

## 6.2b Homework: Tongue Twisters Equations

Use the scatter plots about the tongue twisters to answer each question below.

1. Explain why the slope of each line is different.
2. What does the slope of each line represent?
3. How long does each tongue twister take per person?

Tongue Twister A:

Tongue Twister B:

Tongue Twister C:

Tongue Twister D:

4. What else do you need to write an equation for each line of fit?
5. Write down the y-intercept for each tongue twister.

Tongue Twister A:

Tongue Twister B:

Tongue Twister C:

Tongue Twister D:

6. Write an equation for each line that you could use to predict how much time( $y$ ) it would take for  $x$  number of people to say each tongue twister. Use the slope and y-intercepts that you found previously.

Tongue Twister A:

Tongue Twister B:

Tongue Twister C:

Tongue Twister D:

7. Explain how you would use your equations to predict how long it would take 18 people to say a tongue twister. Similarly, explain how you can use the equation to determine how many people could say a tongue twister in 70 seconds.
9. Use your equation to predict how long it would take 25 people to say Tongue Twister D and Tongue Twister B.
10. Use your equation to predict how many people could say Tongue Twister D in 100 seconds.

## 6.2c Self-Assessment: Section 6.2

Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept.

Skill/Concept	Beginning Understanding	Developing Skill and Understanding	Deep Understanding, Skill Mastery
1. Know that a line of best fit is a linear model that shows the relationship between two variables.			
2. Draw a line of best fit for linear models.			
3. Determine how outliers affect a line of best fit.			
4. Informally assess the model fit by judging the closeness of the data points to the line.			
5. Write an equation for the line of best fit.			
6. Explain the meaning of the slope and $y$ -intercept in context.			
7. Use the equation of a linear model to solve problems.			

How did you use the following practice standards in this section?



## Section 6.3 Construct and Interpret Two-Way Frequency Tables to Analyze Categorical Data

### Section Overview:

At the beginning of this section students are introduced to a new type of random variable – a categorical random variable. Up to this point in the chapter, students have been studying quantitative random variables. Quantitative random variables have a cardinal numerical value. Categorical random variables are those that represent some quality or name. Categorical data is often represented and summarized in a two-way frequency table. In this section, students learn what a two-way frequency table is and how to read it. They complete two-way frequency tables by filling in missing data. As the section progresses, students begin to formally interpret the frequency tables. They calculate and analyze relative frequencies (for rows, columns, and the entire table) to describe possible associations between the two variables and use these associations to make decisions. Finally, students conduct a survey of their own involving categorical random variables, summarize their data in a two-way frequency table, and analyze the data to determine if an association exists between the two variables of interest.

### Concepts and Skills to be mastered:

*By the end of this section students should be able to:*

1. Know the difference between quantitative and categorical random variables.
2. Read and understand a two-way frequency table.
3. Construct a two-way frequency table for categorical data.
4. Calculate and analyze relative frequencies (for rows, columns, and the entire table) to describe possible associations between the two variables and to make decisions.

### 6.3a Class Activity: Construct Two-Way Frequency Tables using Categorical Data

There are two different types of random variables when looking at bivariate data; **quantitative random variables** and **categorical random variables**. So far in this chapter, we have been studying **quantitative random variables**. Quantitative random variables can be counted or measured. For example, we can count the number of assists and rebounds that a player on Izuhmi's team had during the team. We can count the amount that Jenny made in tips each day. We can measure a person's shoe size and their height. We can measure the amount of time it takes to say a tongue twister. A **categorical random variable** represents a quality or a name. Suppose we were interested in determining if there is an association between a person's gender and whether or not that person has pierced ears. We would interview people and classify them as male or female and as yes (ears pierced) or no (ears not pierced). Suppose we were interested in whether a person's favorite color is associated with their favorite holiday. We would categorize a person according to their favorite color (red, orange, yellow, etc.) and their favorite holiday (Christmas, Thanksgiving, Halloween, Hanukah, etc.)

**Directions:** Determine if the following random variables represent data that is Quantitative or Categorical.

1. Gender of babies born in the Riverton Hospital for the month of June
2. Thickness of the plastic for various types of water bottles
3. Favorite ice cream flavor chosen from the following options; chocolate, vanilla, or strawberry
4. The number of pages you can read of your favorite book before you fall asleep

In the previous sections we summarized and displayed quantitative data using a **scatter plot**. In this section, we will summarize and display categorical bivariate data using a **two-way frequency table**. A two-way frequency table is "two-way" because each bivariate data entry is composed of an ordered pair from two categorical random variables.

Suppose we were interested in whether there is an association between a person's gender (male/female) and whether or not they smoke (smoker/non-smoker). The following ordered pairs are possible outcomes for our experiment:

(female, non-smoker) (female, smoker) (male, non-smoker) (male, smoker)

The table is a "frequency" table because the cell entries count the number of data points that fall into each combination of categories.

In this section, we will construct two-way frequency tables and analyze the tables to determine if there is an association between the two variables of interest.

5. Carlos enjoys spending time with his friends. He feels sad when one of his friends cannot hang out with him. Often when one of his friends cannot hang out with him it is because they are either doing their chores or they cannot stay out late at night. Carlos notices that it tends to be the same group of friends that have curfews on school nights who also have chores to do at home. He wonders, “In general, do students at my school who have chores to do at home tend to also have curfews at night?”

Carlos decides to conduct an experiment to help answer his question. He randomly surveys 52 students at his school, asking each student if they have a curfew and if they have to do household chores. He organizes his findings into the frequency table below.

	Has A Curfew	No Curfew	Total
Has Chores	26	9	
No Chores	5	12	
Total			

**Directions:** Use the table to answer each question below.

- How many students have a curfew and have chores?
- How many students have no curfew and have chores?
- How many students have no curfew and no chores?

It is also possible to calculate the frequencies for “Total” column and “Total” row. These frequencies represent the total count of one variable at a time.

- Find the frequencies for the Total column and Total row by adding up the numbers in each column and row. Write these numbers in the table above.
- How many of the students surveyed have chores?
- How many of the students surveyed have a curfew?

You can also calculate how many total students that were surveyed by adding up the frequencies in the “Total” row and “Total” column.

- Add the entries in the Total row and the Total column and put this number in the cell in the bottom left corner. Does this number match how many students that Carlos said he was going to survey?

6. Emina loves to eat tomatoes from her garden in Salt Lake City. She asked her friend Renzo, “Don’t you just love tomatoes?” Renzo crinkled his nose and replied, “Ew, tomatoes gross me out! When I see them in the grocery store, I just keep on walking.” Renzo’s response prompted Emina to think, “I don’t buy tomatoes at the grocery store either, because I grow them in my garden. The tomatoes from my garden are delicious, whereas grocery store tomatoes look less appealing to me. I wonder if there is an association between enjoying tomatoes and having a garden at home.”

She decides to survey 100 randomly selected Salt Lake City vegetable eating residents and asks each of them two questions: 1. Do you primarily obtain your vegetables at the grocery store (including food pantry), the farmer’s market, or your home garden (assume they grow tomatoes in their home garden)? 2. Do you like tomatoes? Her results are summarized in the table below.

	Grocery Store	Farmer’s Market	Home Garden	Total
Likes Tomatoes	50	4	12	
Dislikes Tomatoes	30	1	3	
Total				

- Fill in the frequencies for the Total column and Total row in the table.
- Check to make sure that you found the above frequencies correctly by finding the total number of people surveyed.
- How many people get their tomatoes at the farmer’s market and dislike tomatoes?
- How many people get their tomatoes from a home garden and like tomatoes?
- How many people get their tomatoes from the grocery store?
- How many people like tomatoes?

Emina is not quite sure if her data suggests an association between enjoying tomatoes and having a garden. We will further investigate this relationship in the next section.



7. Use the given information to complete the two-way frequency table about the eating habits of 595 students at Copper Ridge Middle School.

- 190 male students eat breakfast regularly out of 320 total males surveyed.
- 295 students do not eat breakfast regularly
- 165 females do not eat breakfast regularly

- a. Fill in the missing information.

	Male	Female	Total
Eat breakfast regularly			
Do not eat breakfast regularly			
Total			

- b. How many females total were surveyed?
- c. How many people surveyed eat breakfast regularly?
- d. How many people total were surveyed?
- e. How many males surveyed do not eat breakfast regularly?
- f. How many females surveyed eat breakfast regularly?

8. The data given in the table below is about modes of transportation to and from school at Brookside High School.

- a. Fill in the missing information.

	Walk	Car	Bus	Cycle	Total
Male		28			129
Female	46		12	17	92
Total		45	27	69	

- b. How many males ride their bikes to school?
- c. How many females take the bus to school?
- d. How many females were surveyed?
- e. How many students were surveyed?

9. Keane collects data about the number of people who own a smart phone and if they also own an MP3 player. He gives you the following information.

- 25 people surveyed owned smart phones
- 20 people that own a smart phone do not own an MP3 player
- 9 people do not own smart phones but they do own an MP3 player
- 24 people do not own an MP3 player

a. Design and complete a two-way frequency table to show the following information.


b. How many people did Keane survey?

c. How many people own a smart phone and an MP3 player?

d. How many people own MP3 players?

### 6.3a Homework: Construct a Two-Way Frequency Table

1. In Miss Marble's music collection there are...
  - 208 songs in total
  - She has 150 songs in her "Workout Music" playlist
  - 162 of the songs in the total music collection are Pop songs
  - 38 Classical songs are in her "Music for Studying" playlist
- a. Complete the table for about the Miss Marble's music collection.

	Workout Music	Music for Studying	Totals
Classical			
Pop			
Totals			

- b. How many total songs are in her "Music for Studying" playlist?
  - c. How many classical songs are in her "Workout Music" playlist?
2. Laura was driving home from school and texting her mom at the same time. She did not notice that she was speeding and a police officer pulled her over and gave her a traffic citation. She wonders if there is an association between people who regularly text while driving and if they have received a traffic citation in the last 2 years. She conducts a survey among 50 drivers and records some data in the table below.
  - a. Fill in the missing information in the frequency table below.

	Regularly Texts While Driving	Never Texts While Driving	Totals
No traffic citations			
Has received a traffic citation in the last two years.	18	5	
Totals	25		50

- b. How people regularly text while driving?
- c. How many people have no traffic citations and regularly text while driving?

3. Paul tosses a dice and spins a coin 150 times as part of an experiment. He records 71 heads and a six 21 times. On 68 occasions, he gets neither a head nor a six. Complete the table.

	Six	Not a Six	Totals
Head			
Tail			
Totals			

a. How many times did he toss a tails and a six?

b. How many times did he toss a heads?

4. The 300 members of a tennis club are classified by gender and whether or not they are over 18. You are given the following information about the members of the club.
- 36 are under 18 and female
  - 159 are over 18 and male
  - 180 are male

a. Design and complete a two-way table to show this information.


b. How many members of the club are female?

c. How many member of the club are over 18 and female?

5. Susan loves social media and is interested in at what age people prefer different social media outlets. She groups people into the following age groups, middle school age, high school age, and college age. She then asks 75 people what their favorite form of social media is, Twitter, Instagram, or Facebook.
- a. Fill in the missing information in the frequency table below.

	Facebook	Instagram	Twitter	Totals
Middle School		5	3	
High School	10	10		27
College		7		24
Total	31		22	

- b. How many Middle School aged people were surveyed?
- c. How many people prefer Instagram?
- d. How many college age people prefer Facebook?
- e. How many high school aged people prefer Twitter?

### 6.3b Class Activity: Interpret Two-Way Frequency Tables

Now that we are comfortable making a two-way frequency table we are going to see what conclusions we can draw from them.

1. Refer back to Carlos' data regarding chores and curfew.

	Has A Curfew	No Curfew	Totals
Has Chores	26	9	35
No Chores	5	12	17
Totals	31	21	52

- a. Analyze the two-way table. What arguments can you make about the data? Use numerical evidence to support your answer.
- b. Is there an association between kids having chores and having a curfew? Use numerical evidence to support your answer.

2. Let's revisit Emina and her tomatoes.

	Grocery Store	Farmer's Market	Home Garden	Totals
Likes Tomatoes	50	4	12	66
Dislikes Tomatoes	30	1	3	34
Totals	80	5	15	100

- a. Analyze the two-way table. What arguments can you make about the data? Use numerical evidence to support your answer.
- b. Is there an association between growing your own tomatoes (having a home garden) and whether or not you like tomatoes?

3. **Eating Breakfast:** In the previous section you made a frequency table about gender and eating breakfast.

	Male	Female	Totals
<b>Eat breakfast regularly</b>	190	110	300
<b>Do not eat breakfast regularly</b>	130	165	295
<b>Totals</b>	320	275	595

- a. Determine if there is an association between gender and whether or not a person eats breakfast regularly.

4. **Pierced Ears:** Eddy wanted to determine whether there is an association between gender and whether or not a person has their ears pierced. He collected data from a random sample of young adults ages 13 – 18.

	Has Pierced Ears	Does not have Pierced Ears	Totals
<b>Male</b>	19	71	<b>90</b>
<b>Female</b>	84	4	<b>88</b>
<b>Totals</b>	<b>103</b>	<b>75</b>	<b>178</b>

- a. Is there an association between gender and whether or not a person has their ears pierced?



### 6.3b Homework: Interpret Two-Way Frequency Tables

1. **Modes of Transportation:** Recall the data gathered from Brookside High School about modes of transportation and gender.

	Walk	Car	Bus	Cycle	Total
Male	34	28	15	52	129
Female	46	17	12	17	92
Total	80	45	27	69	221

**Directions:** Answer the following questions about the data collected:

- a. What percentage of students surveyed take the bus to school?
- b. What percentage of students surveyed are males who walk to school?
- c. Based off of the table above what is the most popular mode of transportation for the sample population. Use numerical evidence to support your answer.
- d. What is the preferred method of transportation for females? Use numerical evidence to support your answer.
- e. What is the preferred method of transportation for males? Use numerical evidence to support your answer.
- f. Is taking the bus more common with males or females?

2. **Cell Phones and MP3 Players:** Recall the two-way table you made in the previous section about Keane's data on Cell Phones and MP3 Players below.

	<b>Owens a smart phone</b>	<b>Does not own a smart phone</b>	<b>Total</b>
<b>Owens an MP3 player</b>	5	9	14
<b>Does not own an MP3 Player</b>	20	4	24
<b>Total</b>	25	13	38

- What percentage of the people surveyed own a smart phone?
  - What percentage of people do not own a smart phone but own an MP3 player?
  - What percentage of people own a smart phone and an MP3 player?
  - Is there an association between owning a smart phone and owning an MP3 player? Use numerical evidence to support your answer.
3. **Music:** Use the two-way frequency table given below about Miss Marbles' music playlists to answer the following question.

	<b>Workout Music</b>	<b>Music for Studying</b>	<b>Totals</b>
<b>Classical</b>	8	38	46
<b>Pop</b>	142	20	162
<b>Totals</b>	150	58	208

- Is there an association between what Miss Marble is doing (exercising or studying) and what she is listening to? Use numerical evidence to support your answer.

4. **Texting While Driving:** Use the two-way given below about texting while driving to answer the following question.

	<b>Regularly Texts While Driving</b>	<b>Never Texts While Driving</b>	<b>Totals</b>
<b>No traffic citations</b>	7	20	27
<b>Has received a traffic citation in the last two years.</b>	18	5	23
<b>Totals</b>	25	25	50

- What percentage of people regularly text while driving?
- What percentage of people have not received a traffic citation in the last two years?
- What percentage of people regularly text and have received a traffic citation in that last two years?
- What percentage of people that never text have no traffic citations?
- What percentage of people who regularly text while driving have received a traffic citation in the last two years?
- Out of all the people who have received a traffic citation in the last two years, what percentage of them text regularly?
- What type of association exists between texting while driving and receiving traffic citations? Use numerical evidence to support your answer.

5. **Social Media:** Use the two-way frequency table given below to answer the question.

	Facebook	Instagram	Twitter	Totals
Middle School	16	5	3	24
High School	10	10	7	27
College	5	7	12	24
Total	31	22	22	75

- a. Analyze the two-way table. What arguments can you make about the data? Use numerical evidence to support your answer.

### 6.3c Class Activity: Conduct a Survey

Is there an association between whether a student plays a sport and whether he or she plays a musical instrument? *\*This problem was adapted from an Illustrative Mathematics task.*

To investigate these questions, ask 20 students in your class to answer the following two questions:

1. Do you play a sport? (yes or no)
2. Do you play a musical instrument? (yes or no)

Record the answers in the table below.

Student Name	Sport?	Musical Instrument?
1		
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20		

3. Summarize the data into a clearly labeled frequency table.

Use the tables that you made above to answer the following questions.

4. What percentage of students play a sport and a musical instrument?
5. What percentage of students that play a sport also play a musical instrument?
6. What percentage of students that do not play a sport play a musical instrument?
7. What percentage of musical instrument players do not play a sport?
8. Based on the class data, do you think there is an association between playing a sport and playing an instrument? Use numerical evidence to support your answer.

### 6.3d Self-Assessment: Section 6.3

Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept.

<b>Skill/Concept</b>	<b>Beginning Understanding</b>	<b>Developing Skill and Understanding</b>	<b>Deep Understanding, Skill Mastery</b>
1. Know the difference between quantitative and categorical random variables.			
2. Read and understand a two-way frequency table.			
3. Construct a two-way frequency table for categorical data.			
4. Calculate and analyze relative frequencies (for rows, columns, and the entire table) to describe possible associations between the two variables and to make decisions.			